

Entropy as a function of mass

The Sackur-Tetrode formula,

$$S(E, V, N) = k_B N \left[\frac{3}{2} \ln \left(\frac{4\pi m E V^{2/3}}{3h_0^2 N^{5/3}} \right) + \frac{5}{2} \right],$$

predicts that

$$S_{\text{Kr}} - S_{\text{Ar}} = \frac{3}{2} k_B N \ln \left(\frac{m_{\text{Kr}}}{m_{\text{Ar}}} \right).$$

Meanwhile, the masses of a mole of Krypton and a mole of Argon are

$$m_{\text{Kr}} N_A = 83.80 \text{ gr} \quad \text{and} \quad m_{\text{Ar}} N_A = 39.948 \text{ gr},$$

where N_A is Avogadro's number. So the prediction is that

$$S_{\text{Kr}} - S_{\text{Ar}} = \frac{3}{2} k_B N (0.7409).$$

Or, if \mathcal{S} represents the entropy per mole,

$$\mathcal{S}_{\text{Kr}} - \mathcal{S}_{\text{Ar}} = \frac{3}{2} k_B N_A (0.7409) = 9.239 \text{ J/K}.$$

The data in Ihsan Barin, *Thermochemical Data of Pure Substances*, third edition (VCH Publishers, New York, 1995), pages 76 and 924, are

temperature	\mathcal{S}_{Kr}	\mathcal{S}_{Ar}	$\mathcal{S}_{\text{Kr}} - \mathcal{S}_{\text{Ar}}$
300 K	164.213 J/K	154.974 J/K	9.239 J/K
2000 K	203.647 J/K	194.407 J/K	9.240 J/K